UNIVERSITY OF SASKATCHEWAN: A FOUR-PART ARTICLE

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Summary of Parts 1–4

Whilst most investigators using Fisher’s p may still be confident that they are using a
tried and trusted statistic, others are becoming less certain. Their doubts are well justified.
Generally speaking, the p-statistic works well wherever there is an actual or implied diffuse
null hypothesis, but in Part 1 ‘Countering the p-statistic fallacy’ (see pp. 107–116) we show
that where that null hypothesis is precise, the two-sided p-statistic is commonly misinterpreted.

It is also shown in Part 1 that the single-parameter case of the Schwarz-inspired Bayesian
information criterion (BIC), which is well known to be unduly parsimonious, can be remedied
by introducing certain additional but clearly needed penalty terms, which in turn can be seen
to coalesce into a simple function of T (the large sample limiting case of Student’s t).

The relevance of this new information criterion (IC) is confirmed by several features. First,
that it is a simple function of the T-statistic only. A simple transformation of this new IC also
provides a realistic reinterpretation for Fisher’s p. Finally, even when it is generalised to D
free parameters, it is still for almost all practical purposes intermediate in size between the BIC
itself and the corresponding, but insufficiently parsimonious, Akaike’s AIC.

In Part 2 ‘A reference Bayesian hypothesis test’ (see pp. 117–125), we develop a reference
Bayesian hypothesis test which is fully compatible with the single-parameter case of this new
IC. An important role is played here by a hitherto rather neglected (and initially purely empirical)
law of numbers (see Benford (1938), which itself had been based on Newcomb (1881)). When
the T-statistic is observed to be equal to one, that reference Bayesian test is indifferent between
the null and alternative hypotheses. When the new IC is extended to small samples, as a function
of Student’s t-statistic, another important role is played by Fisher’s p; this time in setting an
upper bound to the false discovery rate, regardless of the number of degrees of freedom involved.

In Part 3 ‘Examining an empirical data set’ (to appear in Math. Scientist 37), a set of 1294
regression slopes from a biodiversity survey of tropical landscape mosaics in two hemispheres
(see Gillison et al. (2010)) is used to provide empirical support for the new IC, our earlier
theoretical findings are confirmed, and certain additional conclusions are drawn, including two
in particular that were initially unexpected.

In Part 4 ‘Do we even need to specify a prior measure at H0?’ (to appear in Math. Scientist
37), the approximate results derived in the three earlier parts are supplemented by exact results
that can be obtained using a somewhat similar approach, but one that dispenses entirely with

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the need for any explicit null hypothesis. Finally, we suggest some likely consequences of the recognition that, when the implied null hypothesis is precise, much smaller values of $p$ than currently envisaged are needed to supply any useful false discovery rate.

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